

## **Elasticity solution of thick laminated cylindrical panel with piezoelectric layer under dynamic loading**

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### **Abstract**

As a result of two characteristics, i.e. the direct piezoelectric effect and the inverse piezoelectric effect, piezoelectric materials are widely used in hydro-and electro-acoustics, communications and measurement technology. In recent years the novel usages of them as distributed sensors and actuators in active structure control as noise attenuation, shape control and vibration suppression have attracted serious attention. On the other hand, composite laminates are well known for their high stiffness and strength . Therefore, the integration of piezoelectric materials and structural composites has become the subject of focus in the area of smart materials and structures and numerous papers on this subject have been published.

The theories of plates and shells coupled with piezoelectricity theory were applied to piezoelectric sensor and actuator design [1]. System equations for piezoelectric shell vibrations were derived, using Hamilton's principle and linear piezoelectricity [2,3]. The piezoelectric solutions to long cylindrical panel and shell structures were also presented [4,5,6] . Elasticity solution of anisotropic thick laminated cylindrical panels subjected to dynamic loading was obtained by author [7].

In this paper, the elasticity solution of axisymmetric cross-ply laminated panel with piezoelectric layer is presented. The shell panel is simply supported at four sides and is subjected to asymmetric loading. The highly coupled partial differential equations (p.d.e.) are reduced to ordinary differential equations (o.d.e.) with variable coefficients by means of trigonometric

function expansion in circumferential and axial directions. The resulting ordinary differential equation are solved by Galerkin finite element method. Finally two and three layered panels with piezoelectric layer are solved and the results are compared with latest published results.

## References

- [1]. Lee P.C.Y. and Yu J.D. (1996), Governing equations of piezoelectric plates with graded properties across the thickness, Proc. Annual IEEE Int. freq. control symp. ,623-631.
- [2]. Tzou H.S. and Zhong J.P. (1993), Electromechanics and vibrations of piezoelectric shell distributed systems. J Dyn syst. Meas control 115(3), 506-517.
- [3]. Tzou HS and Zhong JP (1994), Linear theory of piezoelectric shell vibrations, Jsound Vib. 175(1), 77-88.
- [4]. Chen C-Q, Shen Y-P, and Wang X-M (1996), Exact solution for orthotropic cylindrical shell with piezoelectric layers under cylindrical bending, Int. J. Solids struct. 33(30), 4481-4494.
- [5]. Dumir P.C., Dube G.P., and Kapuria S. (1997), Exact piezoelastic solution of simply-supported orthotropic circular cylindrical panel in cylindrical bending, Int. J. solids struct. 34(6), 685-702.
- [6]. Kapuria S., Sengupta S., and Dumir P.C. (1997), Three-dimensional solution for simply-supported piezoelectric cylindrical shell for axisymmetric load, Compu. Methods in Appl. Mech. Eng. 140(1-2), 139-155.
- [7]. M. Shakeri, A. Alibiglu, and M.R. Eslami (2002 ), Elasticity solution for thick laminated anisotropic cylindrical panels under dynamic load, J. Mech. Eng. Sci. Vol. 216 Part C, I Mech E.